

F-2

Hall Ticket Number:

| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|

CE221 (R18)

B.TECH. DEGREE EXAMINATION, SEPTEMBER-2024

Semester IV [Second Year] (Supplementary)

MATHEMATICS - III

Time: Three hours

Maximum Marks: 60

Answer Question No.1 compulsorily. (12 x 1 = 12)

Answer One Question from each unit. (4 x 12 = 48)

1. Answer the following:

- (a) Find the Laplace transform of $\cos(2t + 3)$. CO1
- (b) Write first shifting property for Laplace transform. CO1
- (c) Write Laplace transform of periodic function. CO1
- (d) Define Fourier transform of $f(x)$. CO2
- (e) Define Fourier cosine transform of $f(x)$. CO2
- (f) Define inverse Fourier sine transform of $f(x)$. CO2
- (g) Write $\Delta(\cos x)$. CO3
- (h) Write Newton's forward interpolation formula. CO3
- (i) Write Lagrange's interpolation formula. CO3
- (j) Write Simpson's 1/3rd formula. CO4
- (k) Explain Euler's formula. CO4
- (l) Write Poisson's equation. CO4

UNIT - I

2. (a) Find the Laplace transform of the function

$$f(t) = |t-1| + |t+1|, t \geq 0. \quad (6M) \text{ CO1}$$

(b) Evaluate $\int_0^{\infty} t e^{-3t} \sin t dt$ (6M) CO1

(OR)

3. (a) Find the Laplace transform of the full-wave

rectifier $f(t) = E \sin \omega t, 0 < t < \frac{\pi}{\omega}$, having period $\frac{\pi}{\omega}$. (6M) CO1

(b) Find the inverse transform of $\frac{4s+5}{(s-1)^2(s+2)}$. (6M) CO1

UNIT – II

4. Solve $(D^3 - 3D^2 + 3D - 1)y = t^2e^t$ given that $y(0) = 1$, $y'(0) = 0$, $y''(0) = -2$. CO2

(OR)

5. (a) Find the Fourier transform of

$$f(x) = \begin{cases} 1 & \text{for } |x| < 1 \\ 0 & \text{for } |x| \geq 1 \end{cases}$$

Hence evaluate $\int_0^{\infty} \frac{\sin x}{x} dx$. (6M) CO2

- (b) Find the Fourier cosine transform of

$$f(x) = \begin{cases} \cos x, & 0 < x < a \\ 0, & x \geq a \end{cases} \quad (6M) \text{ CO2}$$

UNIT – III

6. (a) Find the positive root of $x^4 - x = 10$ correct to three decimal places, using Newton-Raphson method. (6M) CO3
- (b) Solve the equations $10x + y + z = 12$, $2x + 10y + z = 13$, $2x + 2y + 10z = 14$ by Gauss- Seidel method. (6M) CO3

(OR)

7. From the following table, estimate the number of students who obtained marks between 40 and 45: CO3

| | | | | | |
|------------------|-------|-------|-------|-------|-------|
| Marks: | 30-40 | 40-50 | 50-60 | 60-70 | 70-80 |
| No. of Students: | 31 | 42 | 51 | 35 | 31 |

UNIT – IV

8. (a) Evaluate $\int_0^6 \frac{dx}{1+x^2}$ by using trapezoidal rule by taking $h = 1$. (6M) CO4

- (b) Find by Taylor's series method the value of y at $x = 0.2$ for $\frac{dy}{dx} = 2y + 3e^x$, $y(0) = 0$. (6M) CO4

(OR)

9. (a) Using Euler's method, find an approximate value of y corresponding to $x = 1$ given that $y' = x + y$ and $y = 1$ when $x = 0$. (6M) CO4
- (b) Apply Runge-Kutta method, to find an approximate value of y when $x = 0.2$ in steps of 0.1 if $y' = x + y^2$, $y_0 = 1$. (6M) CO4

CE221 (R18)

F-2

Hall Ticket Number:

| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|

CE221 (R20)

B.TECH. DEGREE EXAMINATION, SEPTEMBER-2024

Semester IV [Second Year] (Supplementary)

MATHEMATICS - III

Time: Three hours

Maximum Marks: 70

Answer Question No.1 compulsorily. (14 x 1 = 14)

Answer One Question from each unit. (4 x 14 = 56)

1. Answer the following:

- (a) Find the Laplace transform of $f(t) = \sin t$. CO1
- (b) State the change of scale property of Laplace transform. CO1
- (c) Define Laplace transform of $f(t)$. CO1
- (d) Find the Inverse Laplace transform of $\left(\frac{1}{s^2+a^2}\right)$. CO2
- (e) Define Inverse Fourier transform. CO2
- (f) Find the Fourier sine transform of $f(x) = e^{-x}$, $x > 0$ CO2
- (g) Find $L[y^{(1)}(t)]$. CO3
- (h) Write $\frac{dy}{dx}$ at $x = x_0$, using Newton's forward difference. CO3
- (i) Prove that $\Delta = E - 1$. CO3
- (j) Write Newton's iterative formulae for $f(x) = 0$. CO4
- (k) Explain Taylor's series method. CO4
- (l) Write Simpson's 1/3rd rule. CO4
- (m) Write the advantage of R-K method of order 4. CO4
- (n) Write Laplace equation. CO4

UNIT - I

2. (a) Find the Laplace transform of (i) $t \sin t$

(ii) $\frac{e^{-at} - e^{-bt}}{t}$ (7M) CO1

(b) Find the Inverse Laplace transform of

$\tan^{-1}\left(\frac{2}{s}\right)$. (7M) CO1

(OR)

3. (a) Apply the Convolution theorem, find
 $L^{-1}\left(\frac{s}{(s^2+a^2)(s^2+b^2)}\right)$. (7M) CO1
 (b) Find $L(t \sin 3t \cos 2t)$. (7M) CO1

UNIT – II

4. (a) Solve $\frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 3y = e^{-t}$, given $y(0) = 1$ and $y'(0) = 1$ using Laplace transform method. (7M) CO2
 (b) Solve $y^{11} + 2y' - 3y = \sin t$, given that $y(0) = 0$ and $y'(0) = 0$ using Laplace transform method. (7M) CO2

(OR)

5. (a) Find the Fourier cosine transform of $f(x) = e^{-ax}$, $x > 0$. (7M) CO2
 (b) Find the Fourier transform of
 $f(x) = \begin{cases} 1 - |x| & \text{for } |x| \leq 1 \\ 0 & \text{for } |x| > 1 \end{cases}$ (7M) CO2

UNIT – III

6. (a) Find a real root of the equation $x e^x = \cos x$, correct to three decimals. (7M) CO3
 (b) Construct Newton's forward interpolation polynomial for the following values, hence find $f(4)$ (7M) CO3

| | | | | |
|------|---|---|---|----|
| x | 0 | 1 | 2 | 3 |
| f(x) | 1 | 2 | 1 | 10 |

(OR)

7. (a) Find Lagrange's interpolation polynomial $f(x)$, given that (7M) CO3

| | | | | |
|------|-----|-----|-----|-----|
| x | 0 | 2 | 3 | 6 |
| f(x) | 648 | 704 | 728 | 792 |

- (b) Find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ at $x = 1.0$, given that (7M) CO3

| | | | | | | |
|---|-----|-------|-------|-------|-------|-------|
| x | 1.0 | 1.2 | 1.4 | 1.6 | 1.8 | 2.0 |
| y | 0.0 | 0.128 | 0.544 | 1.296 | 2.432 | 4.000 |

UNIT – IV

8. (a) Evaluate $\int_0^1 \frac{dx}{1+x^2}$ using Simpson's 1/3rd rule, taking $h = \frac{1}{4}$. (7M) CO4
 (b) Apply R-K method of order 4, compute $y(0.2)$ taking $h = 0.1$ if $\frac{dy}{dx} = x+y^2$, $y(0) = 1$. (7M) CO4

(OR)

9. Solve the Poisson's equation $\nabla^2 u = -10(x^2 + y^2 + 10)$ over the square mesh with sides $x = 0 = y$, $x = 3 = y$ with $u(x, y) = 0$ on the boundary and mesh length is 1. CO4

CE221 (R20)

F-2

Hall Ticket Number:

| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|

CE221 (R20)

B.TECH. DEGREE EXAMINATION, MAY-2024

Semester IV [Second Year] (Regular & Supplementary)

MATHEMATICS-III

Time: Three hours

Maximum Marks: 70

Answer Question No.1 compulsorily. (14 x 1 = 14)

Answer One Question from each unit. (4 x 14 = 56)

1. Answer the following:
- (a) State change scale property of Laplace transforms. CO1
 - (b) Find $L\{te^{2t}\}$. CO1
 - (c) State convolution theorem. CO1
 - (d) Define transforms of derivative property of Laplace transforms. CO2
 - (e) Define Fourier sine transform. CO2
 - (f) Define inverse Fourier transform. CO2
 - (g) Write the Newton's forward difference formula for finding first order derivative. CO3
 - (h) Write Newton Raphson iterative formula. CO3
 - (i) Write Newton forward interpolation formula. CO3
 - (j) Evaluate $\Delta(x^2)$, $h = 1$. CO4
 - (k) Write the Laplace equation. CO4
 - (l) Write Simpson's 1/3rd rule. CO4
 - (m) Write Taylor series for solving ODE. CO4
 - (n) Write Euler's method iterative formula. CO4

UNIT - I

2. (a) Find $L\{te^{-3t} \sin 2t\}$. (7M) CO1
- (b) Find the Laplace transform of the full-wave rectifier $f(t) = E \sin \omega t$, $0 < t < \pi / \omega$, having period π / ω . (7M) CO1

(OR)

3. (a) Find $L^{-1}\left\{\frac{1}{(s+1)(s+2)^2}\right\}$. (7M) CO1
 (b) Using Convolution theorem evaluate $L^{-1}\left\{\frac{1}{(s^2+1)(s^2+9)}\right\}$. (7M) CO1

UNIT – II

4. Using transformation method, find the solution of the initial value problem $y'' - 3y' + 2y = 4e^{2t}$ with $y(0) = -3$ and $y'(0) = 5$. CO2

(OR)

5. (a) Find the Fourier transform of $f(x) = \begin{cases} 1 & \text{for } |x| < 1 \\ 0 & \text{for } |x| > 1 \end{cases}$. (7M) CO2

- (b) Find the Fourier cosine transform of $f(x) = \begin{cases} x & \text{for } 0 < x < 1 \\ 2-x & \text{for } 1 < x < 2 \\ 0 & \text{for } x > 2 \end{cases}$. (7M) CO2

UNIT – III

6. (a) Solve the equations $2x + y + z = 16$, $2x + 9y + 3z = 29$, $2x + 4y + 8z = 34$ by Gauss-Seidel method. (7M) CO3
 (b) Compute using Newton's backward difference formula, from the following table. (7M) CO3

| | | | | | | |
|---|----|----|------|----|------|------|
| x | 6 | 8 | 10 | 12 | 14 | 16 |
| y | 10 | 19 | 32.5 | 54 | 89.5 | 15.4 |

(OR)

7. Using Lagrange's interpolation formula evaluate $f(9)$, from the following table: CO3

| | | | | | |
|------|-----|-----|------|------|------|
| x | 5 | 7 | 11 | 13 | 17 |
| f(x) | 150 | 392 | 1492 | 2366 | 5202 |

UNIT – IV

8. (a) Evaluate $\int_0^6 \frac{dx}{1+x^2}$ using trapezoidal, Simpson's $\frac{1}{3}$ rd rule, $h = 1$. (7M) CO4
 (b) Using Euler's method find $y(0.2)$ given that $\frac{dy}{dx} = x - y^2$, $y(0) = 1$, $h = 0.1$ (7M) CO4

(OR)

9. Using Runge-Kutta method of order 4, find $y(0.1)$, $y(0.2)$ given that $\frac{dy}{dx} = x + 4y$, $y(0) = 1$, taking $h = 0.1$ CO4

CE221 (R20)

F-2

Hall Ticket Number:

| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|

CE221 (R20)

B.TECH. DEGREE EXAMINATION, NOVEMBER-2023

Semester IV [Second Year] (Supplementary)

MATHEMATICS - III

Time: Three hours

Maximum Marks: 70

Answer Question No.1 compulsorily. (14 x 1 = 14)

Answer One Question from each unit. (4 x 14 = 56)

1. Answer the following:

- (a) State multiplication by t property of Laplace transforms. CO1
- (b) Find $L\{te^{-t}\}$. CO1
- (c) Find $L^{-1}\left\{\frac{1}{((s-2)^2)}\right\}$. CO1
- (d) Define inverse Fourier sine transform. CO2
- (e) Define Fourier cosine transform. CO2
- (f) Define Fourier transform. CO2
- (g) Write the Newton's backward difference formula for finding first order derivative. CO3
- (h) Evaluate $\nabla(x^2)$, $h = 1$. CO3
- (i) Write Newton backward interpolation formula. CO3
- (j) Evaluate $\Delta(e^x)$, $h = 1$. CO3
- (k) Write the Poisson's equation. CO4
- (l) Write Trapezoidal rule. CO4
- (m) Write Simson's 1/3rd rule. CO4
- (n) Explain R-K method. CO4

UNIT - I

- 2. (a) Find $L\left\{\frac{\cos 2t - \cos t}{t}\right\}$. (7M) CO1
- (b) Using Laplace transform, evaluate $\int_0^{\infty} te^{-2t} \sin 3t dt$. (7M) CO1

(OR)

3. (a) Using partial fractions find $L^{-1}\left\{\frac{1}{(s+1)(s+2)(s+3)}\right\}$. (7M) CO1
- (b) Using Convolution theorem find $L^{-1}\left\{\frac{1}{(s^2+1)(s^2+4)}\right\}$. (7M) CO1

UNIT – II

4. Using Laplace transform method, find the solution of the initial value problem $y'' + y = t$ with $y(0) = 1$ and $y'(0) = 0$. CO2

(OR)

5. (a) Find the Fourier transform of (7M) CO2

$$f(x) = \begin{cases} 1 - x^2 & \text{for } |x| \leq 1 \\ 0 & \text{for } |x| > 1 \end{cases}$$

- (b) Find the Fourier sine transform of (7M) CO2

$$f(x) = \begin{cases} 4x & \text{for } 0 < x < 1 \\ 4 - x & \text{for } 1 < x < 4 \\ 0 & \text{for } x > 4 \end{cases}$$

UNIT – III

6. (a) Evaluate $\sqrt{5}$ using Newton Raphson method correct up to 3 decimal places. (7M) CO3
- (b) From the following table estimate the number of students who obtained marks between 30 and 45 (7M) CO3

| Marks | 30-40 | 40-50 | 50-60 | 60-70 | 70-80 |
|----------------|-------|-------|-------|-------|-------|
| No.of students | 31 | 42 | 51 | 35 | 31 |

(OR)

7. Using Lagrange's interpolation formula evaluate $f(7)$, from the following table CO3

| | | | | | |
|------|----|----|----|----|----|
| x | 1 | 5 | 6 | 9 | 13 |
| f(x) | 24 | 38 | 47 | 64 | 72 |

UNIT – IV

8. (a) Evaluate $\int_0^6 \frac{dx}{1+x^4}$ using trapezoidal, Simpson's $\frac{1}{3}$ rd rule, take $h = 1$. (7M) CO4
- (b) Using Euler's method find $y(0.2)$ given that $\frac{dy}{dx} = x + y^2$, $y(0) = 1$, $h = 0.1$. (7M) CO4

(OR)

9. Using Runge-Kutta method of order 4, find $y(0.1)$, $y(0.2)$ given that $\frac{dy}{dx} = x^2 - y^2$, $y(0) = 1$, taking $h = 0.1$. CO4

CE221 (R20)

Hall Ticket Number:

| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|

File-2

CE221 (R20)

B.TECH. DEGREE EXAMINATION, JULY-2023

Semester IV [Second Year] (Regular & Supplementary)

MATHEMATICS - III

Time: Three hours

Maximum Marks: 70

Answer Question No.1 compulsorily. (14 x 1 = 14)

Answer One Question from each unit. (4 x 14 = 56)

1. Answer the following:

- (a) State linearity property of Laplace transform. CO1
- (b) What is the Laplace transform of $e^{at} \sin bt$. CO1
- (c) State convolution theorem. CO1
- (d) Define Fourier transform of a function $f(x)$. CO2
- (e) If $F(s)$ and $G(s)$ are Fourier transforms of $f(t)$ and $g(t)$ respectively then find $F\{af(x) + bg(x)\}$. CO2
- (f) Define inverse Fourier cosine transform of a function $f(x)$. CO2
- (g) Write Newton's backward interpolation formula. CO3
- (h) Evaluate $\Delta(x^2 + 2x)$. CO3
- (i) State Lagrange's interpolation formula for $(x_0, y_0), (x_1, y_1), (x_2, y_2)$. CO3
- (j) State trapezoidal rule to evaluate definite integral. CO4
- (k) Write the formula for k_2 in 4th order R-K method. CO4
- (l) Explain Euler's iteration scheme. CO4
- (m) Write a note on forward differences. CO3
- (n) Write Laplace equation. CO4

UNIT - I

2. (a) Find the Laplace transform of $e^{2t} + 4t^3 - 2 \sin 3t + 3 \cos 3t$ (7M) CO1
- (b) Using Laplace transform evaluate $\int_0^{\infty} \frac{\sin t}{t} dt$ (7M) CO1

(OR)

3. (a) Find inverse Laplace transform of $\frac{1}{s^2+2s+5}$ (7M) CO1
 (b) Using Convolution theorem find inverse Laplace transform of $\frac{s^2}{s^4-a^4}$ (7M) CO1

UNIT - II

4. Using Laplace transform solve the differential equation $x'' - 2x' + x = e^t$, $x = 2$, $x' = -1$ at $t = 0$. CO2

(OR)

5. (a) Find Fourier sine transform of xe^{-ax} (7M) CO2
 (b) Find the Fourier transform of $f(x) = \begin{cases} 1, & |x| < a \\ 0, & |x| > a \end{cases}$ (7M) CO2

UNIT - III

6. (a) Using Gauss seidel method solve the equation $27x + 6y - z = 85$, $x + y + 54z = 110$, $6x + 15y + 2z = 72$ (7M) CO3
 (b) Evaluate $\Delta^2 \left(\frac{1}{x^2 + 5x + 6} \right)$ (7M) CO3

(OR)

7. (a) The population of a town in the decimal census was given below in thousands. Estimate the population for the year 1895. (7M) CO3

| | | | | | |
|----------------|------|------|------|------|------|
| Year (x) | 1891 | 1901 | 1911 | 1921 | 1931 |
| Population (y) | 46 | 66 | 81 | 93 | 101 |

- (b) Find y' and y'' at $x = 0$ from the following data (7M) CO3

| | | | | | | |
|---|---|---|----|---|---|---|
| x | 0 | 1 | 2 | 3 | 4 | 5 |
| y | 4 | 8 | 15 | 7 | 6 | 2 |

UNIT - IV

8. (a) Using Simpson's rule evaluate $\int_0^1 \frac{1}{1+x^2} dx$ (7M) CO4
 (b) Using Taylor's series method find $y(0.4)$ for the differential equation $y' = x^2 + y^2$ given $y(0) = 0$. (7M) CO4

(OR)

9. Using Runge- Kutta 4th order method find $y(1.2)$ for the differential equation $y' = x - y$, $y(1) = 0.4$, take $h=0.1$ CO4

CE221 (R20)

Hall Ticket Number:

| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|

file-2

CE221 (R20)

B.TECH. DEGREE EXAMINATION, JANUARY-2023

Semester IV [Second Year] (Supplementary)

MATHEMATICS - III

Time: Three hours

Maximum Marks: 70

Answer Question No.1 compulsorily. (14 x 1 = 14)

Answer One Question from each unit. (4 x 14 = 56)

1. Answer the following:

- (a) Find the Laplace transform of (a^t) . CO1
- (b) State the First shifting property of Laplace transform. CO1
- (c) State Convolution theorem. CO1
- (d) Find the Inverse Laplace transform of $\left(\frac{1}{s+a}\right)$. CO1
- (e) Define Fourier transform of $f(x)$. CO2
- (f) Find the Fourier Sine transform of $f(x)$. CO2
- (g) Find the Fourier Cosine transform of $f(x) = e^{-x}$, $x > 0$. CO2
- (h) Write Newton's Iterative formulae for \sqrt{N} . CO3
- (i) Evaluate $\Delta(e^x)$, $h = 1$. CO3
- (j) Write Lagrange's Interpolation formula. CO3
- (k) Write Trapezoidal Rule. CO4
- (l) Explain Euler's Method. CO4
- (m) Write Elliptic Equation. CO4
- (n) Classify the equation $u_{xx} + u_{xy} - 2u_{yy} = 0$. CO4

UNIT - I

- 2. (a) Find the Laplace Transform of $\frac{\text{Cos}at - \text{Cos}bt}{t}$ (7M) CO1
- (b) If $f(t) = t$, $0 < t < a$
 $= 2a - t$, $a < t < 2a$, Find $L(f(t))$ (7M) CO1

(OR)

3. (a) Find the Inverse Laplace transform
 $\frac{1}{2} \log \left(\frac{s^2+b^2}{s^2+a^2} \right)$ (7M) CO1
- (b) Apply convolution theorem to evaluate
 $L^{-1} \left(\frac{s}{(s^2+a^2)(s^2+b^2)} \right)$ (7M) CO1

UNIT – II

4. (a) Solve the differential equation using Laplace transform method, if $y'' - 3y' + 2y = 4t + e^{3t}$, $y(0) = 1$ and $y'(0) = 1$. (7M) CO2
- (b) Solve $y'' - y = a \cos ht$, $y(0) = 0$ & $y'(0) = 0$ using Laplace transform method. (7M) CO2

(OR)

5. (a) Find the Fourier transform of
 $f(x) = \begin{cases} 1 - x^2, & |x| \leq 1 \\ 0, & |x| > 1 \end{cases}$ (7M) CO2
- (b) Find the Fourier Sine transform of
 $f(x) = \begin{cases} \sin x, & 0 \leq x \leq a \\ 0, & x \geq a \end{cases}$ (7M) CO2

UNIT – III

6. (a) Solve by Gauss Siedal method, the equations
 $20x + y - 2z = 17$, $3x + 20y - z = -18$ and
 $2x - 3y + 20z = 25$ (7M) CO3
- (b) Construct Newton's forward interpolation polynomial $y = f(x)$ for the following data (7M) CO3

| | | | | |
|---|---|---|---|----|
| x | 4 | 6 | 8 | 10 |
| y | 1 | 3 | 8 | 16 |

(OR)

7. (a) Apply Lagrange's formula to find the value of y when $x = 10$, given that (7M) CO3

| | | | | |
|---|----|----|----|----|
| x | 5 | 6 | 9 | 11 |
| y | 10 | 13 | 14 | 16 |

- (b) Given that

| | | | | | | | |
|---|-------|-------|-------|-------|--------|-------|--------|
| x | 1.0 | 1.1 | 1.2 | 1.3 | 1.4 | 1.5 | 1.6 |
| y | 7.989 | 8.403 | 8.781 | 9.129 | 9.4511 | 9.750 | 10.031 |

- Find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ at $x = 1.1$ (7M) CO3

UNIT – IV

8. (a) Integrate Numerically $\int_0^{\pi/2} \sin \theta d\theta$ taken 10 equal parts. (7M) CO4
- (b) Find the value of y when $x = 0.1$ if
 $\frac{dy}{dx} = x^2 + y^2$, $y(0) = 0$ using Taylor's series method. (7M) CO4

(OR)

9. Solve the Laplace Equation $u_{xx} + u_{yy} = 0$
 Under the conditions ($h = 1$, $k = 1$)
 $u(0, y) = 0$, $u(4, y) = 12 + y$ for $0 \leq y \leq 4$
 $u(x, 0) = 3x$, $u(x, 4) = x^2$ for $0 \leq x \leq 4$. CO4

CE221 (R20)

Hall Ticket Number:

file-2

| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|

CE221(R20)

B.TECH. DEGREE EXAMINATION, OCTOBER-2022

Semester IV [Second Year] (Regular)

MATHEMATICS-III

Time: Three hours

Maximum Marks: 70

Answer Question No.1 compulsorily. (14 x 1 = 14)

Answer One Question from each unit. (4 x 14 = 56)

I. Answer the following in brief:

- (a) Define Laplace transform of a function $f(x)$. CO1
- (b) State first shifting property of Laplace transform of a function $f(x)$. CO1
- (c) Find the inverse Laplace transform of $\frac{4s+4}{4s^2-9}$. CO1
- (d) Define Fourier cosine transform of $f(x)$. CO2
- (e) If $F(s)$ is the Fourier transform of $f(x)$ then find $F\{f(ax)\}$. CO2
- (f) Define inverse Fourier sine transform of a function $f(x)$. CO2
- (g) Write Newton's forward interpolation formula. CO3
- (h) Evaluate $\nabla\left(\frac{1}{(x+2)}\right)$. CO3
- (i) For what type of data Lagranges interpolation is applicable? CO3
- (j) State Simpsons rule to evaluate definite integral. CO4
- (k) Write the formula for k in R-K 4th order method. CO4
- (l) Write Poisson's equation. CO4
- (m) Write the formula to find first order derivative using forward differences. CO4
- (n) Which method is used to solve Laplace equation? CO4

UNIT - I

2. (a) Find the Laplace transform of $e^{-3t}(2 \cos 5t - 3 \sin 5t)$ (7M) CO1

(b) Evaluate the integral by using Laplace

transform $\int_0^{\infty} \frac{e^{-t} - e^{-2t}}{t} dt$ (7M) CO1

(OR)

3. (a) Find Inverse Laplace transform of $\frac{s}{s^4 + s^2 + 1}$ (7M) CO1

(b) Using convolution theorem find the inverse

Laplace transform of $\frac{s^2}{(s^2+4)(s^2+9)}$ (7M) CO1

UNIT - II

4. Solve the differential equation by applying Laplace transform $y'' + 2y' - 3y = \sin t$, $y = y' = 0$ when $t = 0$. CO2

(OR)

5. (a) Find Fourier transform of $f(x)$ defined by

$$f(x) = \begin{cases} 1-x^2, & |x| \leq 1 \\ 0, & |x| > 1 \end{cases} \quad (7M) \text{ CO2}$$

(b) Find Fourier cosine transform of $\frac{e^{-ax}}{x}$ (7M) CO2

UNIT - III

6. (a) Using Newton-Raphson method find the root of the equation $f(x) = e^x - 3x$ that lies between 0 and 1. (7M) CO3

(b) Construct the difference table for the given data (7M) CO3

| | | | | | |
|------|-----|-----|-----|-----|-----|
| x | 0 | 1 | 2 | 3 | 4 |
| f(x) | 1.0 | 1.5 | 2.2 | 3.1 | 4.6 |

(OR)

7. (a) Using Newton forward and backward interpolation find $f(0.5)$, $f(3.5)$ for the data (7M) CO3

| | | | | |
|------|---|---|---|----|
| x | 0 | 1 | 2 | 3 |
| f(x) | 1 | 3 | 7 | 13 |

(b) Find the Lagrange's interpolation polynomial for the given data $f(0) = 2$, $f(1) = 3$, $f(2) = 12$, $f(5) = 147$. (7M) CO3

UNIT - IV

8. (a) Using trapezoidal rule evaluate $\int_0^1 \frac{1}{1+x} dx$ and compare with traditional method. (7M) CO4

(b) Using Eulers method solve for y at $x = 2$ for $\frac{dy}{dx} = 3x^2 + 1$, $y(1) = 2$, take $h=0.25$. (7M) CO4

(OR)

9. (a) Solve the differential equation $y' = x - y$ given that $y(1) = 0.4$. Find $y(1.2)$ using Runge-Kutta method. (7M) CO4

(b) What is the classification of the solutions of the partial differential equation $f_{xx} + 2f_{xy} + f_{yy} = 0$. (7M) CO4
